## Oberseminar

## Zahlentheorie und Arithmetische Geometrie

## Dr. Francesc Fité

(Universität Duisburg-Essen)

## "Sato-Tate groups of abelian surfaces and CM elliptic k-curves"

The Sato-Tate group ST(A) of an abelian variety A defined over a number field k of dimension g is a compact real Lie subgroup of the unitary symplectic group USp(2g) that conjecturally governs the limiting distribution of the Frobenius conjugacy classes attached to A. It is well known that there exist 3 possibilities for the Sato-Tate group of an elliptic curve. I will present a classification result which establishes that for an abelian surface defined over a number field the Sato-Tate group is limited to a list of 52 possibilities, exactly 34 of which can occur if  $k = \mathbb{Q}$ . Then I will consider the question concerning the existence of a number field  $k_0$  over which each of the 52 possibilities can be attained by a certain abelian surface of defined over  $k_0$ . An affirmative answer to this question will be obtained as a consequence of the study of fields of definition of certain CM elliptic k-curves. The talk will report on joint works with Kedlaya, Rotger, Sutherland, and Guitart.

Donnerstag 23.06.2016 12:00 Uhr, Raum a410 Hauptgebäude der Leibniz Universität Hannover Alle Interessierten sind herzlich eingeladen.

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