

# Oberseminar

zur

## Algebra und Algebraischen Kombinatorik

Prof. Dr. Wolfgang Willems

(Otto-von-Guericke-Universität Magdeburg)

### "Lie-type-like groups"

Let  $K$  be an algebraically closed field of characteristic  $p > 0$  dividing the order of the finite group  $G$ . We shall discuss relations between the block structure of the group algebra  $KG$  and the structure of the group  $G$ . By a result of Harris in 1985, the group algebra is indecomposable as a two-sided ideal (i.e.  $KG = B_0 =$  the principal block) if and only if  $p$  is odd and  $O_{p'}(G) = F^*(G)$  (generalized Fitting group) or  $p = 2$ ,  $O_{p'}(G) = 1$  and all components of  $G$  are of type  $M_{22}$  or  $M_{24}$  (Mathieu groups). In the talk we consider the case  $KG = B_0 \oplus B_1$  where the  $B_i$  are two-sided indecomposable ideals and  $B_1$  is the full matrix algebra  $(K)_{|G|_p}$  (i.e.  $KG$  consists of the principal block  $B_0$  and a particular block  $B_1$  of defect zero). For non-solvable groups and  $p \geq 5$ , it turns out that this is exactly the case if  $G$  is a finite simple group of Lie type in defining characteristic  $p$ .

Montag, 15.12.2014

ab 14:15 Uhr, Raum a410

Hauptgebäude der Leibniz Universität Hannover

Alle Interessierten sind herzlich eingeladen.

gez. Prof. Dr. C. Bessenrodt

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